

# Hydrolysis of hard cations, a molecular dynamics study

UMR 8587  
Evry University (France)  
Supervisor: Thierry Cartailier  
co-supervising: Marc Souaille

Magali Duvail  
PhD Thesis started on October 2004

UMR 8587  
CEA Saclay DPC/SECR  
co-supervising: Pierre Vitorge



## Context

Aqueous Radio-Chemistry in nuclear fuel cycles, waste disposals and environment

## Objectives

- Modelling the hydration of  $\text{La}^{3+}$ , a cation analogue to lanthanides(III) fission products,  $\text{Am}^{3+}$ ,  $\text{Cm}^{3+}$  and  $\text{Pu}^{3+}$
- Parametrization of a model potential for molecular dynamics simulations.

## Methodology

### Potential:

#### 1. Definition

Model potential:

$$E = V^{\text{Coul}} + V^{\text{pol}} + V^{\text{LJ}} + V^{\text{TF}}$$

- The Coulomb electrostatic term is given by:

$$V_i^{\text{Coul}}(r_{ij}) = \frac{e^2 q_i q_j}{4\pi\epsilon_0 r_{ij}}$$

- Polarisation...

$$V^{\text{pol}} = -\frac{1}{2} \sum_i (\vec{\mu}_i \cdot \vec{E}_i) \quad \vec{\mu}_i = \alpha \vec{E}_i \quad \vec{E}_i = \vec{E}_i^{\text{ext}} + \frac{1}{4\pi\epsilon_0} \sum_{j \neq i} (\vec{T}_j \mu_j)$$

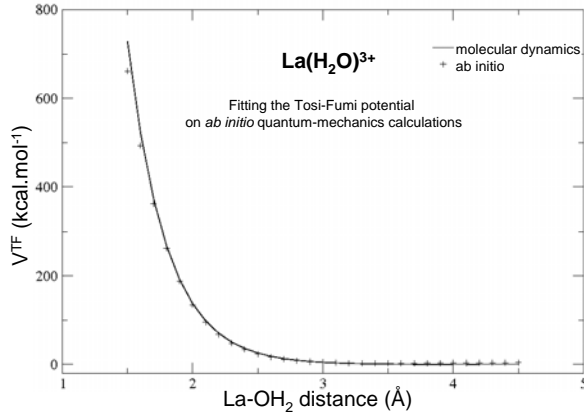
- Short-range interactions were accounted for by using 12-6 Lennard-Jones Potential:

$$V_{ij}^{\text{LJ}}(r_{ij}) = 4\epsilon_{ij} \left[ \left( \frac{\sigma_{ij}}{r_{ij}} \right)^{12} - \left( \frac{\sigma_{ij}}{r_{ij}} \right)^6 \right]$$

- and Tosi-Fumi Potential [1,2] with parameters fitted in the present work

$$V_{ij}^{\text{TF}}(r_{ij}) = a \exp(-br_{ij}) - \frac{c}{r_{ij}^6} - \frac{d}{r_{ij}^8} - \frac{e}{r_{ij}^{10}}$$

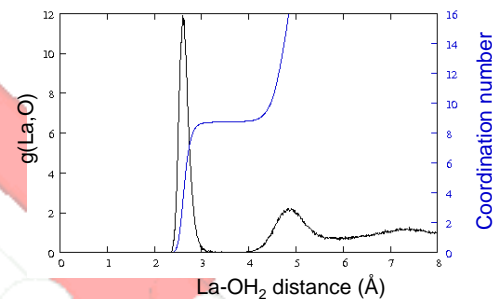
#### 2. Parametrization:



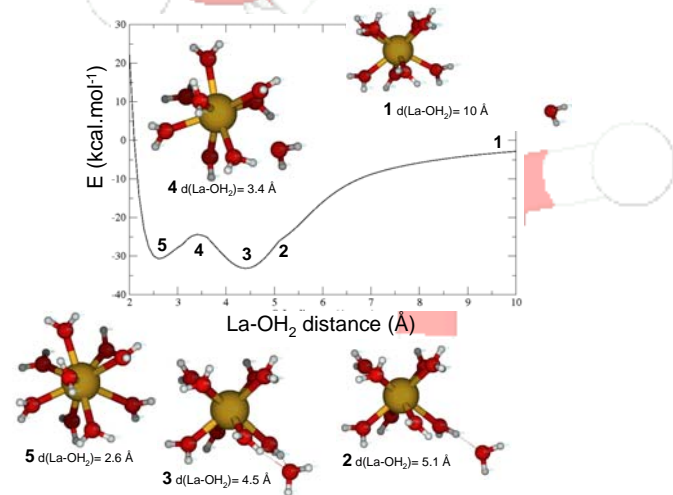
## First results

### 1. Molecular dynamics simulations

- 216 water molecules
- Temperature: 298 K
- Length of the cubic box: 18.643 Å



### 2. Ab initio calculations



## Conclusion

- Parameterization of the Tosi-Fumi potential
- Comparison between molecular dynamics simulations, *ab initio* calculations and published data

	1 <sup>st</sup> shell		2 <sup>nd</sup> shell	
	O-La (Å)	CN	O-La (Å)	CN
Molecular dynamics	2.60 ± 0.01	8.75	4.84 ± 0.01	~16
<i>Ab initio</i> calculations	2.6 ± 0.1	8	4.5 ± 0.1	-
Published data	2.54 ± 0.02 [3]	9.2 ± 1.5 [3]	4.63 [4]	16.0 [4]

## Prospect

- Influence of Temperature on the first shell coordination number of  $\text{La}(\text{H}_2\text{O})_{216}^{3+}$
- Study of  $\text{La}(\text{H}_2\text{O})_8(\text{OH})_2^{2+}$  by *ab initio* calculations

### References:

- [1] F.Fumi, M.Tosi, *J.Phys.Chem.Solids* **25**, 31 (1964)
- [2] M.Tosi, F.Fumi, *J.Phys.Chem.Solids* **25**, 45 (1964)
- [3] P.Allen, J.Bucher, D.Shuh, N.Edelstein, I.Craig, *Inorg.Chem.* **39**,595 (2000)
- [4] C.Clavaguera, R.Pollet, J.Soudan, V.Brenner, J.P.Dognon, *J.Phys.Chem.B.* **109**,7614 (2005)